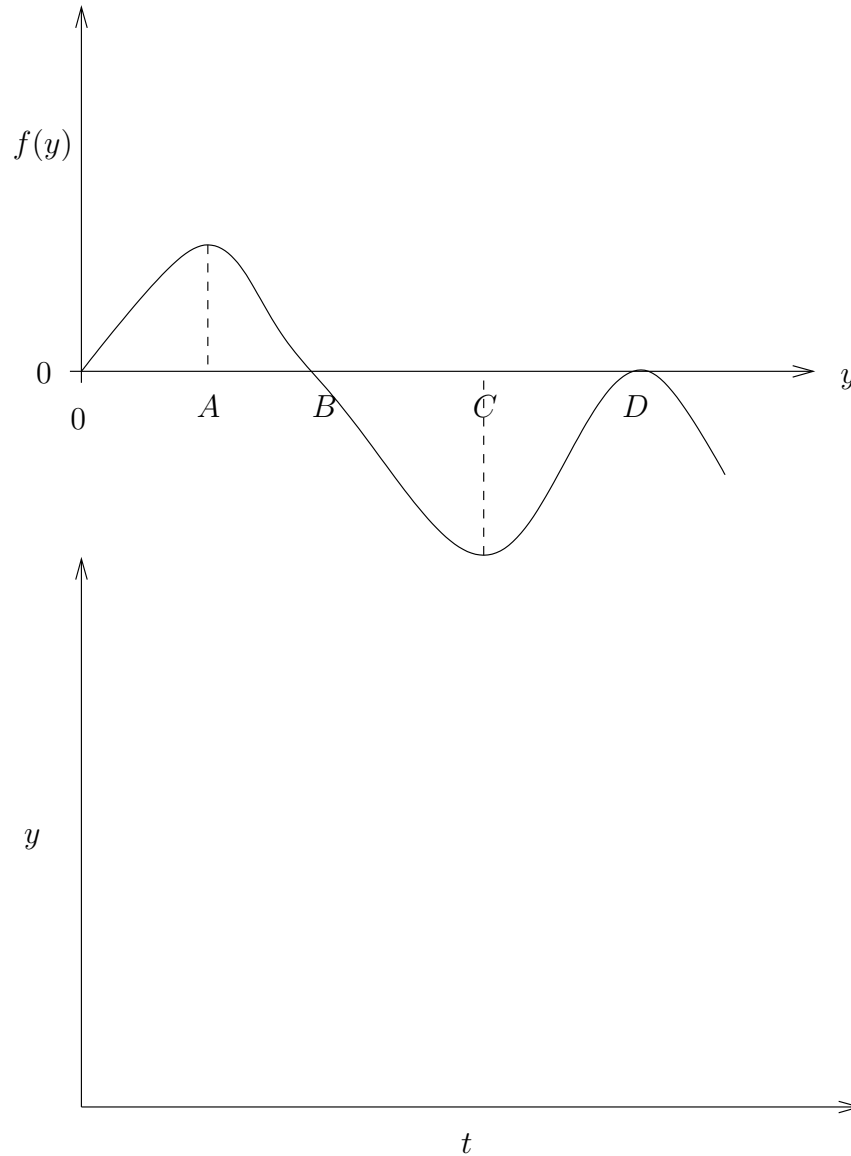
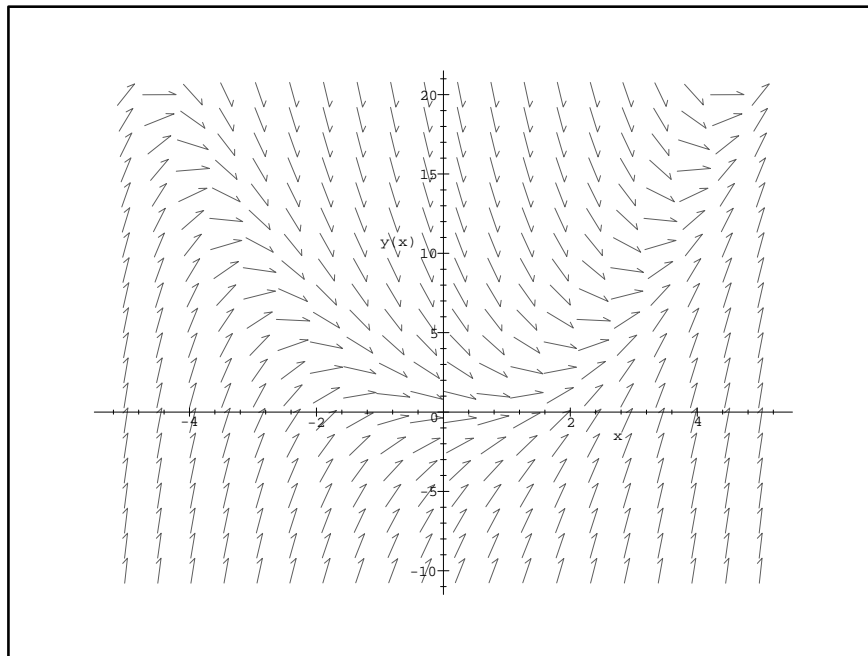


Part I: NO CALCULATORS

1. [10 points] Suppose $y'(t) = F(y(t))$, where the graph of $F(y)$ is given below. Carefully draw the integral curves for this equation. What are the equilibrium solutions? What are their stability types? Describe the initial concavity of the solution curves. Assume $y(t)$ and t are nonnegative.



2. [10 points] The direction field below is from $y' = Ay^2 + Bx^2 + Cy + Dx + E$, where each of the coefficients is either 1, 0 or -1 . Find them.
3. [20 points] Solve the initial value problem $y'' + 2y' - 15y = 0$, $y(0) = 1$, $y'(0) = a$. For which value(s) of a is $\lim_{x \rightarrow \infty} y(x) = 0$?
4. [20 points] Consider the equation $3y^2y' + 2y^3 = x$. This equation can be made linear by using the change of variable $v = y^3$. Do this, then solve the equation for $y(x)$. Hint: $\int ue^u du = (u - 1)e^u + C$.



Math 305

Test 1

Spring 1999

Name: _____ ID #: _____

Part II: CALCULATORS ALLOWED

5. [20 points] A tank has 100 gal. of fresh water. A flow of 2 gal/min of salt water with saliently $1/2$ lbs/gal starts at $t = 0$. The solution in the tank is well mixed and is being drained off at a rate of 1 gal/min. How much salt is in the tank when the volume of water has reached 200 gal.?
6. [20 points] A 32 pound weight is dropped into a tank of fluid 320 feet deep. The weight lands on the tank bottom after 15 seconds. Find the fluid's resistance coefficient k , assuming the resistance is proportional to the speed of the weight. Note: You will not be able to solve for k . Instead set up a function in k whose zero gives the desired value. Graph this function and zoom in on the zero.