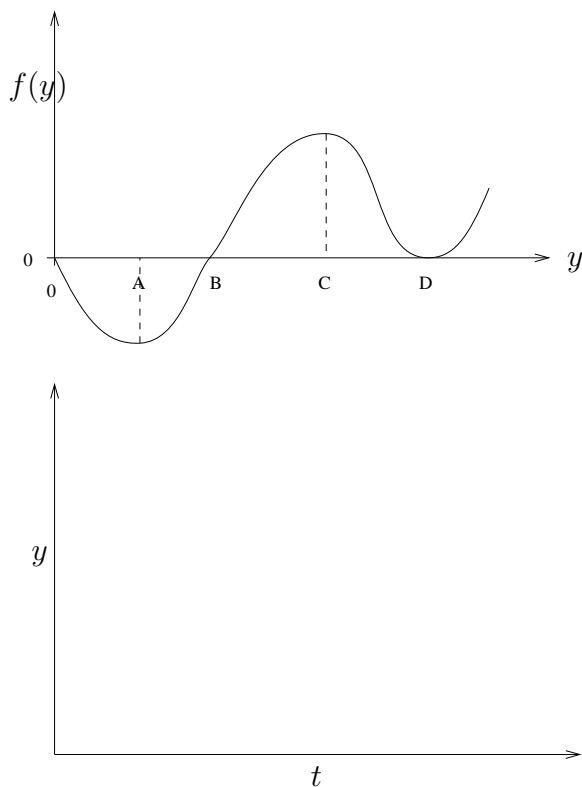
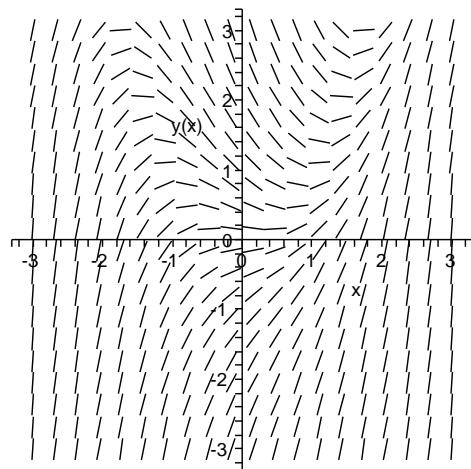
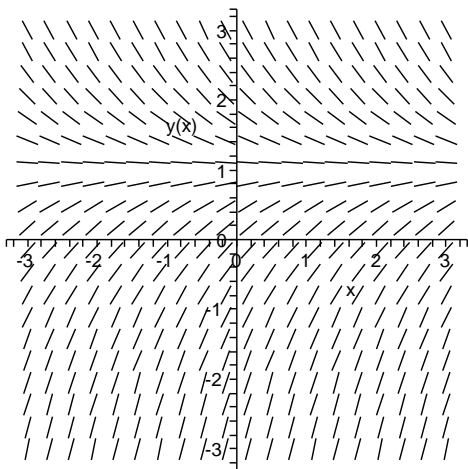
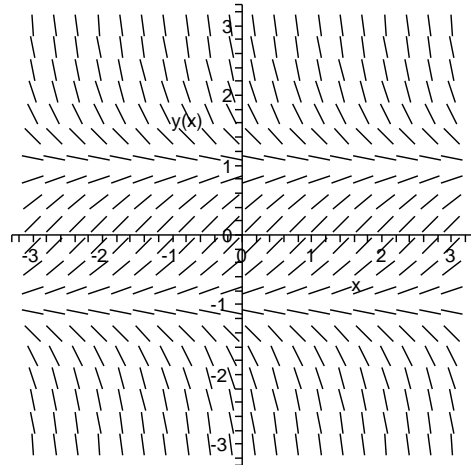
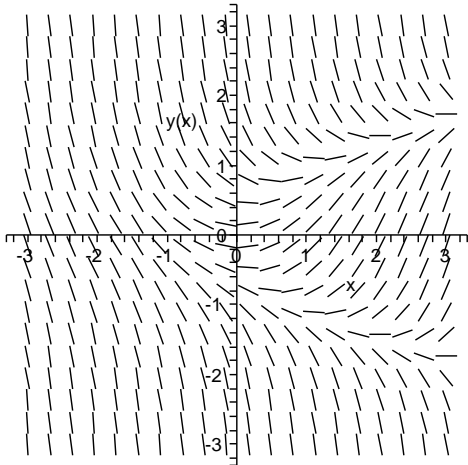
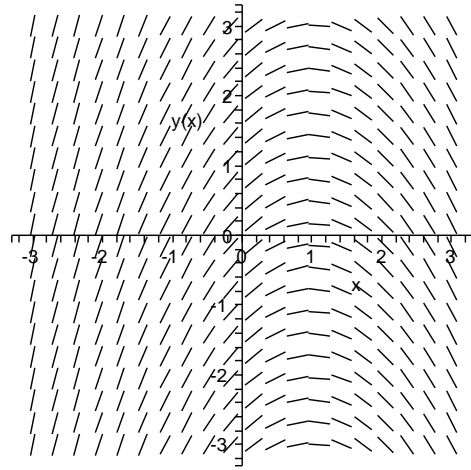
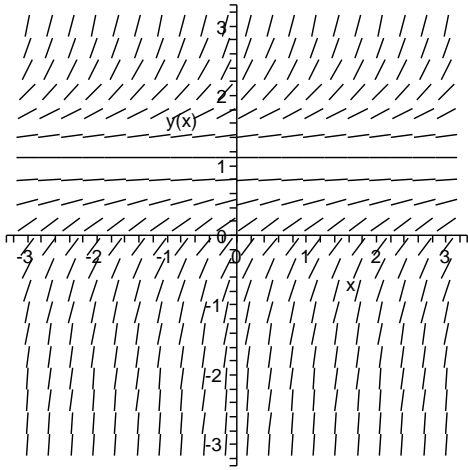


Each problem is worth 20 points.  
NO CALCULATORS

1. Suppose  $y'(t) = f(y)$ , where the graph of  $f(y)$  is given below. Carefully draw the integral curves for this equation. What are the equilibrium solutions? What are their stability types? Describe the initial concavity of the solution curves. Assume  $y(t)$  and  $t$  are nonnegative.



2. Match the differential equation with its direction field. (You get 4 points for each correct match, -2 for each wrong match.)
1.  $y' = y - 2$
  2.  $y' = 2 - y$
  3.  $y' = |y - 2|$
  4.  $y' = y + x$
  5.  $y' = x - y$



3. Find a continuous solution to the initial value problem,  $y' + p(t)y = g(t)$ ,  $y(0) = 1$ , where

$$p(t) = \begin{cases} 1 & t \leq 1 \\ 0 & t > 1 \end{cases}$$

and

$$g(t) = \begin{cases} 0 & t \leq 2 \\ 1 & t > 2 \end{cases}$$

Sketch the graph of your solution,  $y(t)$ , for  $0 \leq t \leq 5$ . Hint:  $y(5) = 3 + 1/e$ .

4. Find the general solution of the differential equation  $(x^2 + y)y' + 2xy = 6x$ . Hint: check for exactness. (You need not solve for  $y$ .)
5. A tank contains 200 gallons of salt water. The initial salinity is .5 lb/gal. The water is then pumped out of the tank, run through a filter, and pumped back in. The flow rate is 5 gallons a minute. The filter removes 30% of the salt. Also, water is evaporating at a rate of 1 gallon per minute. How much salt is left in the tank when the water has all evaporated? Assume the water in the tank is well mixed.