

**Example with repeated eigenvalue with one-dimensional eigenspace.**

$$\begin{aligned}x' &= -5x - y \\ y' &= 4x - y\end{aligned}$$

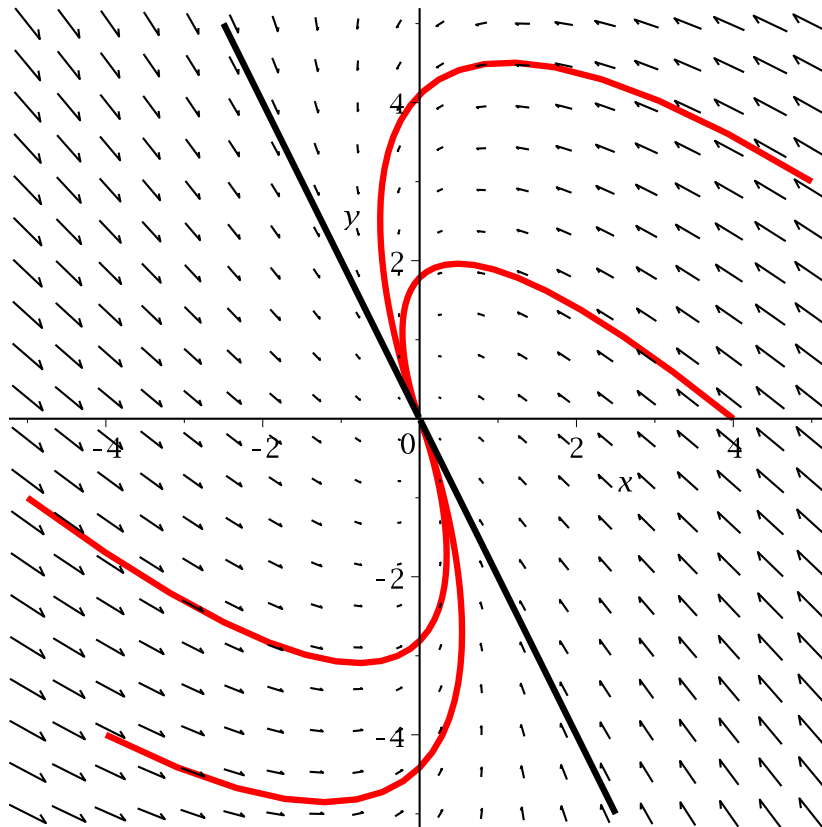
You should check that -3 is the only eigenvalue and that  $[1 \ -2]^T$  is a basis for the one-dimensional eigenspace. Below we plot the vector field and six solution curves. The two solution curves in black show the eigenspace.

```
> with(DEtools):with(plots):
```

```
> solutioncurves := phaseportrait([ D(x)(t) = -5*x(t)-y(t), D(y)(t) = 4*x(t)-y(t)], [x(t), y(t)], t=0..2, [[x(0)=-5, y(0)=-1], [x(0)=5, y(0)=3], [x(0)=4, y(0)=0], [x(0)=-4, y(0)=-4], [x(0)=2.5, y(0)=-5], [x(0)=-2.5, y(0)=5]], linecolor=[red, red, red, red, black, black], color=black, arrows=none, x=-5..5, y=-5..5):
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```
> vectorfield := fieldplot([-5*x-y, 4*x-y], x=-5..5, y=-5..5):
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```
> display(solutioncurves, vectorfield);
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The origin in this case is called an improper node. It is asymptotically stable. It looks like it wants to be a spiral, but could not make up its mind!

