

# ERRATA TO AN INVARIANT OF BASIC SETS OF SMALE FLOWS

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There is an error in [5], which is repeated in [6, 7] and [4, Definition 5.2.5]. The problem is with the definition of *ribbon sets*. With the new definition given below all results are preserved.

Ribbons sets were defined as the local stable manifold of a basic set of saddle type in a Smale flow. However, every local stable manifold has some “thickness”,  $\epsilon > 0$ . But in the proof of Lemma 4.3, which is used to prove Theorem 4.1, one must be able to make arbitrarily many refinements and reorderings of the Markov partition. Hence a local stable manifold need not be invariant. Intuitively, what is needed is an *infinitesimal stable manifold*. Formally, we redefine a ribbon set to be the suspension of a *disjoint* union of local stable manifolds of points in a cross section of the basic set.

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